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## The effect of surfactant charge on micellization behavior

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**Abstract** The influence of the surfactant charge on micellization was studied on sodium *n*-dodecanephosphonates, varying the charge of the surfactant ion from 0 to 2. The effects on the cmc, hydrolysis, micelle composition, and micelle ionization degree were studied. The increase

of one *e* unit in the charge of the surfactant species reduces the cmc by about one order of magnitude.

**Key words** Micelle charge – alkanephosphonates – cmc – micellization – micelle composition

### Introduction

Alkanephosphonates are surfactants which have been scarcely studied. They are salts of a diprotic acid, which enables a study to be made of the effect of increasing the charge of the headgroup between 0 and 2. However, *n*-alkanephosphonic acids are weak [1–3] and the hydrolysis of their salts complicates the interpretation of data. The theoretical interest in the study of these characteristics is evident. Phosphonates have increasing importance in industry as detergent additives [4], inhibitors of corrosion [5], ligands [6], metal extractors [7, 8] and agents of flotation [9]. Therefore, a knowledge of their properties is of great practical interest.

Only a few measurements of the cmc of alkylphosphonates have been reported in literature, limited to the cmc value determined by a single method, such as conductivity or surface tension. However, the phenomena that take place at the cmc have not been investigated in detail, except in a very few cases.

### Experimental

The preparation and purification of *n*-dodecanephosphonic acid (H<sub>2</sub>DP) has been described elsewhere [10].

Mono and disodic *n*-dodecanephosphonate (HNaDP and Na<sub>2</sub>DP) solutions were made by taking a weighed amount of solid acid and neutralizing by the appropriate amount of NaOH solution in double-distilled water. Surface tension measurements were made using a ring-tensiometer (Krüss). Conductivity measurements were performed with an immersion cell and an automatic conductimeter, namely, an Antares II of Instrumentalia. Sealed tubes with Sudan Black B in surfactant solutions of different concentration were left for 1 week in a constant temperature bath, with periodic stirring. Then the tubes were centrifuged and the supernatant absorbance was measured with a Hewlett-Packard Diode Array HP84 52A spectrometer at 600 nm. OH<sup>−</sup> determinations were made with an Orion glass electrode and pH-meter. To determine Na<sup>+</sup> ions, a Na<sup>+</sup> ion-selective electrode Metrohom EA 109 vs. SCE was employed. To determine HDP- and DP<sup>2−</sup> ions, a membrane electrode was made, whose description and performance are described elsewhere [11]. The potentiometric data were analyzed by the usual method described in literature to determine the free and micellized ion concentrations and the micelle ionization degree [12].

Several tubes with different concentration of HNaDP in water were prepared. The Krafft point was determined by recording the temperature at which the surfactant solid dissolved on heating.

When straight lines were obtained, they were treated by the least-squares method. Averages were obtained with the minimum variance linear unbiased estimation method [13]. A confidence level of 0.90 and the Student's *t* distribution function were employed in all error estimations.

## Results

### Monosodium *n*-dodecanephosphonate

Figure 1 shows the HNaDP solubility in water as a function of temperature. The Krafft point obtained from this data was 65 °C. That of monosodium *n*-decanephosphonate is  $29.3 \pm 1.1$  °C [14]. On the basis of the Krafft point, the other experiments were run at 66 °C.

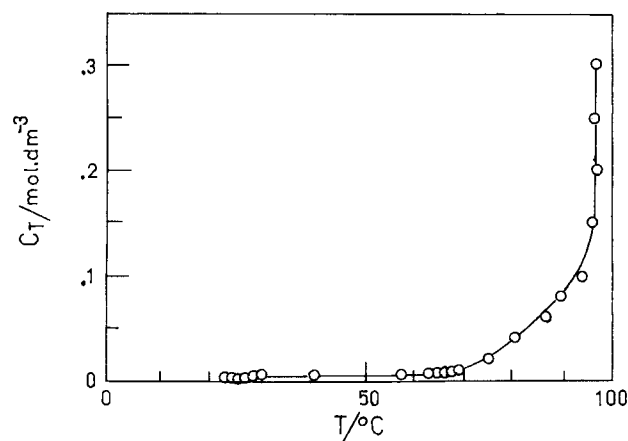


Fig. 1 Solubility of HNaDP in water vs. temperature

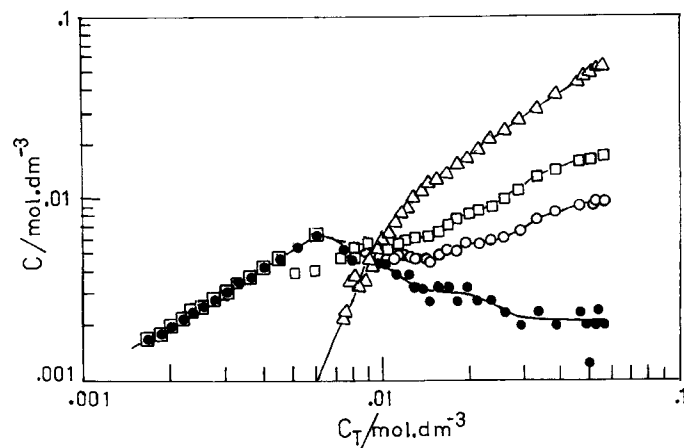


Fig. 2 Concentration of  $\square$ : free  $\text{Na}^+$  ions,  $\bullet$ : free  $\text{HDP}^-$  ions,  $\triangle$ : micelles (on a monomer basis), and  $\circ$ : ionic strength vs. total concentration of HNaDP in water at 66 °C

From the dependence of the surface tension of solutions of HNaDP on the concentration, the determined cmc was  $(6 \pm 0.2) \times 10^{-3} \text{ mol dm}^{-3}$ .

The concentrations of free  $\text{Na}^+$  and  $\text{HDP}^-$  ions at different total concentrations ( $C_T$ ) of the surfactant in water are shown in Fig. 2. The cmc value was  $(6.0 \pm 0.4) \times 10^{-3} \text{ mol dm}^{-3}$  ( $\text{HDP}^-$  electrode) and  $(4 \pm 0.2) \times 10^{-3} \text{ mol dm}^{-3}$  ( $\text{Na}^+$  electrode).

The hydrolysis degree  $\beta = [\text{OH}^-]/C_T$  was plotted in Fig. 3 against the total concentration of the surfactant. The cmc determined in this plot was  $(7.0 \pm 0.2) \times 10^{-3} \text{ mol dm}^{-3}$ . From pH measurements,  $\text{cmc} = (6.7 \pm 0.4) \times 10^{-3} \text{ mol dm}^{-3}$ .

In Fig. 4 the equivalent conductivity vs.  $\sqrt{C_T}$  is shown. The cmc determined on the basis of these data is

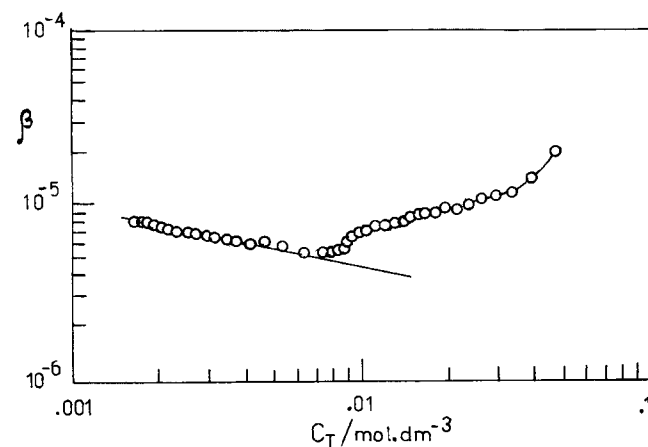


Fig. 3 Degree of hydrolysis of HNaDP vs. concentration in water at 66 °C

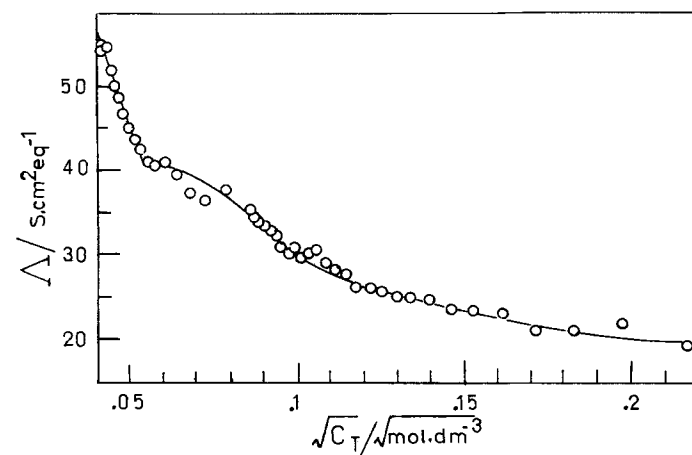


Fig. 4 Equivalent conductivity of HNaDP solutions vs. the square root of total concentration at 66 °C

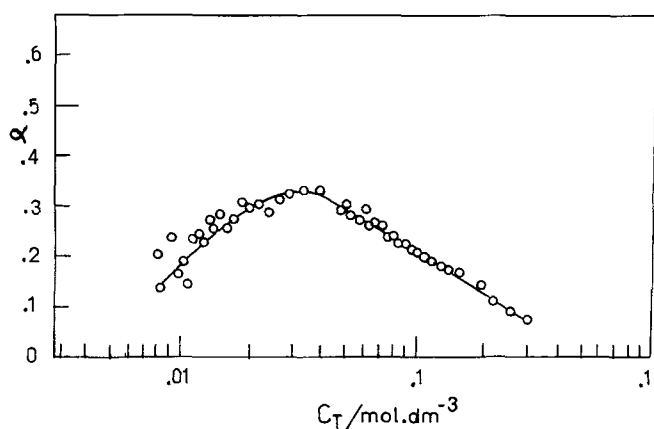


Fig. 5 Micelle ionization degree of HNaDP solutions vs. total concentration at 66°C

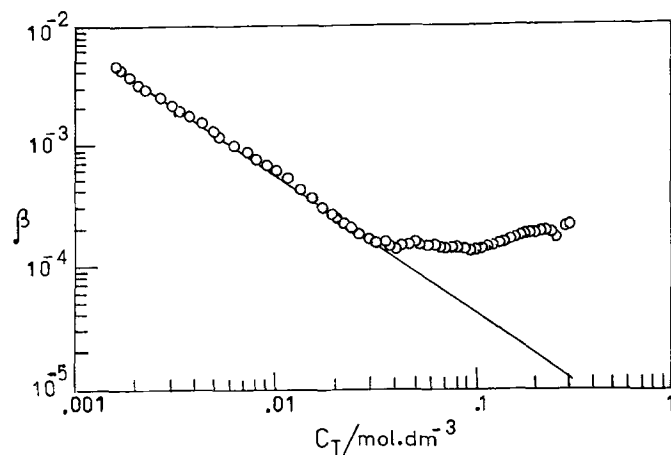


Fig. 7 Degree of hydrolysis of Na₂DP vs. concentration in water at 25°C

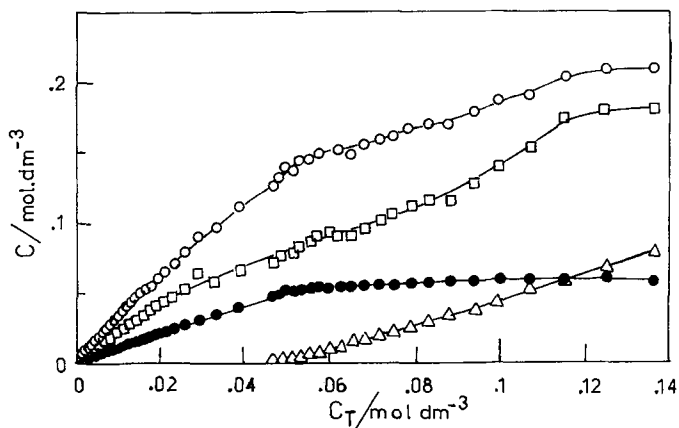


Fig. 6 Concentration of  $\square$ : free  $\text{Na}^+$  ions,  $\bullet$ : free  $\text{DP}^{2-}$  ions,  $\Delta$ : micelles (on a monomer basis), and  $\circ$ : ionic strength vs. total concentration of  $\text{Na}_2\text{DP}$  in water at 25°C

$(5.7 \pm 0.4) \times 10^{-3} \text{ mol dm}^{-3}$ . From specific conductivity,  $\text{cmc} = (7.3 \pm 0.8) \times 10^{-3} \text{ mol dm}^{-3}$ . The equivalent conductivity at infinite dilution of  $\text{NaHDP}$  was  $\Lambda_0 = 96.95 \text{ S cm}^2 \text{ eq}^{-1}$ .

By solubilization of Sudan Black B a value of  $(5.9 \pm 0.3) \times 10^{-3} \text{ mol dm}^{-3}$  for the cmc was found.

Figure 5 shows the effective charge per micellized molecule vs. the total concentration of surfactant.

#### Disodium *n*-dodecanephosphonate

Figure 6 shows the dependence of the free  $\text{Na}^+$  and  $\text{DP}^{2-}$  ions on the total concentration of the surfactant. The cmc was  $(2.6 \pm 0.2) \times 10^{-2} \text{ mol dm}^{-3}$  ( $\text{Na}^+$  electrode) and  $(3.0 \pm 0.2) \times 10^{-2} \text{ mol dm}^{-3}$  ( $\text{DP}^{2-}$  electrode).

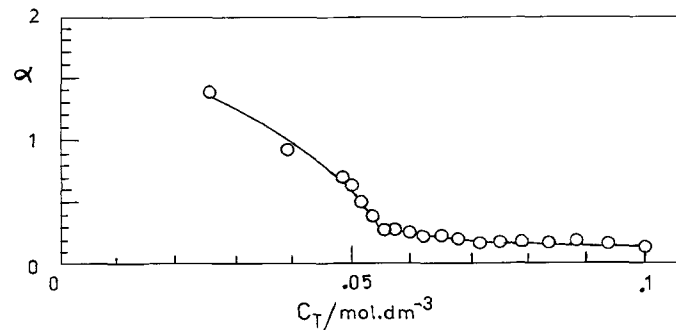


Fig. 8 Micelle ionization degree of  $\text{Na}_2\text{DP}$  solutions vs. total concentration at 25°C

In Fig. 7 the hydrolysis degree of  $\text{Na}_2\text{DP}$  was plotted vs. the total concentration. From this plot,  $\text{cmc} = (3.5 \pm 0.2) \times 10^{-2} \text{ mol dm}^{-3}$ . From  $[\text{OH}^-]$  vs. concentration data,  $\text{cmc} = (3.2 \pm 0.2) \times 10^{-2} \text{ mol dm}^{-3}$ . Sudan Black B solubilization gave  $\text{cmc} = (1.1 \pm 0.3) \times 10^{-2} \text{ mol dm}^{-3}$ . Surface tension measurements gave  $\text{cmc} = (1.3 \pm 0.2) \times 10^{-2} \text{ mol dm}^{-3}$ . Specific conductivity measurements gave  $\text{cmc} = (1.6 \pm 0.8) \times 10^{-2} \text{ mol dm}^{-3}$ , and the same data, plotted as equivalent conductivity, gave  $\text{cmc} = (2.3 \pm 0.8) \times 10^{-2} \text{ mol dm}^{-3}$ .

Figure 8 shows the micellar degree of ionization as a function of concentration. Note that the maximum value of  $\alpha$  is 2 for  $\text{Na}_2\text{DP}$  micelles.

#### Discussion

##### Monosodium *n*-dodecanephosphonate

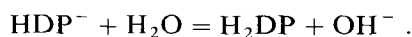
From the various methods employed, the cmc average value of monosodium *n*-dodecanephosphonate at 66°C

obtained by the linear unbiased minimum variance estimation method was:

$$\text{cmc} = (5.80 \pm 0.10) \times 10^{-3} \text{ mol dm}^{-3}.$$

The literature value is  $0.0056 \text{ mol dm}^{-3}$  [15] or  $0.0065 \text{ mol dm}^{-3}$  [16].

Dodecanephosphonic acid has two ionization constants ( $\text{p}K_1 = 3.98$  and  $\text{p}K_2 = 8.42$  [17]). In HNaDP aqueous solutions, there are two species in equilibrium,  $\text{HDP}^-$  and  $\text{H}_2\text{DP}$ . They are related by the hydrolysis equilibrium:



The straight line in Fig. 3 corresponds to a normal hydrolysis of an aqueous solution of a weak acid salt. The separation of the experimental data from the straight line indicates the increased hydrolysis at the cmc. Because of the low solubility, *n*-decanephosphonic acid (formed by the  $\text{HDP}^-$  hydrolysis) dissolves into micelles. In micelles, the unionized  $-\text{PO}_3\text{H}_2$  groups intercalate between charged  $-\text{PO}_3\text{H}^-$  groups. As in  $\text{H}_2\text{DP}$  mesophases [18], the groups in surface must be bound by strong hydrogen bonds. At the same time, the surface charge density is reduced, stabilizing micelles.

The degree of hydrolysis together with the hydrolysis equilibrium, which is applicable to the unmicellized  $\text{HDP}^-$  ions, enabled us to determinate the composition of micelles. The concentration of free (unmicellized)  $\text{H}_2\text{DP}$  was computed by the hydrolysis constant:

$$[\text{H}_2\text{DP}]_{\text{free}} = K_{\text{hid}} [\text{HDP}^-]_{\text{free}} / [\text{OH}^-]_{\text{free}}$$

and the micellized  $\text{HDP}^-$  to micellized  $\text{H}_2\text{DP}$  ratio was computed by

$$R = \frac{[\text{H}_2\text{DP}]_{\text{mic}}}{[\text{HDP}^-]_{\text{mic}}} = \frac{([\text{OH}^-] - [\text{H}_2\text{DP}]_{\text{free}})}{(C_T - [\text{HDP}^-]_{\text{free}})}.$$

This ratio is plotted in Fig. 9 against total concentration. It is seen that between the cmc and  $C_T = 0.036 \text{ mol dm}^{-3}$ , it is almost constant, with an average value of  $(1.03 \pm 0.40) \times 10^{-5}$ . The ratio is  $3.03 \times 10^{-7}$  for dodecyltrimethylammonium hydroxide micelles [19] and  $2.8 \times 10^{-4}$  for sodium palmitate micelles [20]. At  $C_T > 0.036 \text{ mol dm}^{-3}$ , this ratio rises with increasing concentration. This situation is probably associated with a change in micelle structure. As an example, rod-like micelles have more solubilizing capacity than spherical ones [21]. The transition may be facilitated by formation of strong hydrogen bonds between the headgroups.

The distribution constant of  $\text{H}_2\text{DP}$  molecules between micelles and intermicellar solution may be computed by the equation:

$$K_d = \frac{[\text{H}_2\text{DP}]_{\text{mic}}}{[\text{H}_2\text{DP}]_{\text{w}}} = \frac{1000R}{V_{\text{m,HNaDP}} \cdot [\text{H}_2\text{DP}]_{\text{w}}},$$

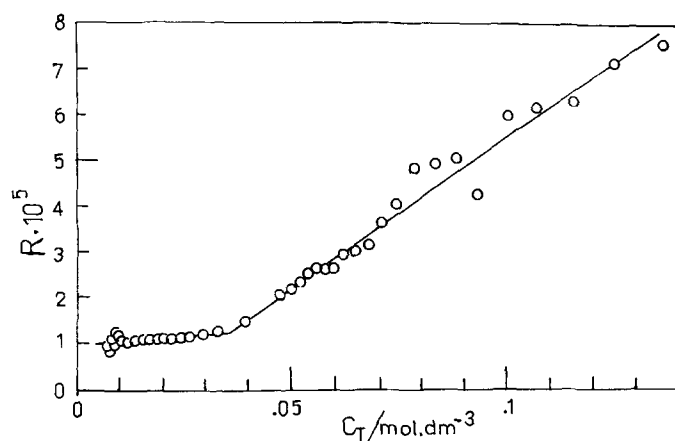


Fig. 9 The micellized  $\text{H}_2\text{DP}$  molecules to micellized  $\text{HDP}^-$  ions ratio vs. total concentration. HNaDP solutions in water at  $66^\circ\text{C}$

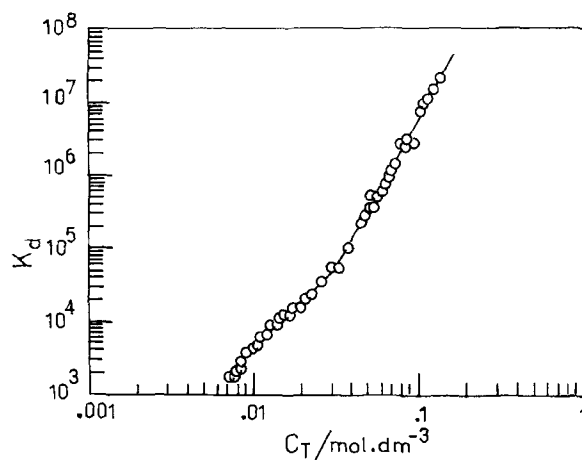


Fig. 10 The distribution constant of  $\text{H}_2\text{DP}$  between HNaDP micelles and water vs. total concentration. HNaDP solutions in water at  $66^\circ\text{C}$

$V_{\text{m,HNaDP}}$  being the partial molar volume of micellized HNaDP. The partial molar volume of micellized  $\text{Na}_2\text{DP}$  is  $240.73 \pm 0.5 \text{ cm}^3 \text{ mol}^{-1}$  at  $21^\circ\text{C}$ , and its temperature coefficient is  $0.001810 \pm 0.000011^\circ\text{C}^{-1}$  [22]. There are no literature data for HNaDP, but a good estimation may be made by subtracting the partial molar volume of the  $\text{Na}^+$  ion ( $-5.7 \text{ cm}^3 \text{ mol}^{-1}$ ) and adding that of  $\text{H}^+$  ion ( $-4.5 \text{ cm}^3 \text{ mol}^{-1}$ ) [23]. This gave  $V_{\text{m,HNaDP}} = 241.9 \pm 0.2 \text{ cm}^3 \text{ mol}^{-1}$  at  $21^\circ\text{C}$ , and  $261.6 \pm 0.2 \text{ cm}^3 \text{ mol}^{-1}$  at  $66^\circ\text{C}$ . The dependence of  $K_d$  with the total concentration is shown in Fig. 10. It may be seen that  $K_d$  increases with  $C_T$ , with a break at  $C_T \approx 0.035 \text{ mol dm}^{-3}$ . This behavior shows that the interaction between  $\text{H}_2\text{DP}$  and micelles changes with concentration. The growth of micelles with

concentration indicates that the micellized headgroups approach each other, giving better opportunities to the formation of inter-headgroup hydrogen bonds. This may increase the capacity of micelles to solubilize  $\text{H}_2\text{DP}$  molecules.

The shape of the conductivity curve in Fig. 5 may be due to the formation of an excess of strongly conducting  $\text{OH}^-$  ions by the micellization hydrolysis.

Figure 7 shows that micelles have an ionization degree ( $\alpha$ ) similar to that of other anionic surfactants near the cmc ( $\alpha \approx 0.2$ ), but differs from them, since  $\alpha$  rises with increasing concentration and passes through a maximum ( $\alpha \approx 0.35$ ) at about  $0.035 \text{ mol dm}^{-3}$ . At higher concentrations the micellar degree of ionization falls which is common in other surfactants. The change in behavior occurs at the same concentration in which both the  $[\text{H}_2\text{DP}]/[\text{HDP}^-]_{\text{mic}}$  ratio and  $K_d$  change their dependence on total concentration. A change in micelle shape, such as a sphere-rod-like transition, must mean that the headgroups approach each other. This situation increases the surface potential and in consequence, more counterions are attached to the micelle Stern layer, thus reducing  $\alpha$ .

#### Disodium *n*-dodecanephosphonate

The average value of the cmc of  $\text{Na}_2\text{DP}$  at  $25^\circ\text{C}$  was

$$\text{cmc} = 0.0257 \pm 0.0008 \text{ mol dm}^{-3}.$$

Literature values are  $0.0177 \text{ mol dm}^{-3}$  [24],  $0.0238 \text{ mol dm}^{-3}$  [15] and  $0.0221 \text{ mol dm}^{-3}$  [16].

Figure 7 shows that hydrolysis increased at the cmc. However, in this case the product of hydrolysis is the  $\text{HDP}^-$  ion. This ion is less soluble than  $\text{DP}^{2-}$ , but much more soluble than  $\text{H}_2\text{DP}$  and solubilizes in micelles. The value of  $\alpha$  was high at the cmc (about 1.4) and diminished with increasing concentration because of the high surface potential which captures  $\text{Na}^+$  ions in the Stern layer, and the very high ionic strength  $I$  (see Fig. 6), which diminishes the Debye length. At  $C_T \approx 0.55 \text{ mol dm}^{-3}$ ,  $\alpha$  reached a more normal value of  $\sim 0.2$ .

The micellized  $\text{HDP}^-$  to  $\text{DP}^{2-}$  ratio was computed in the same manner as in the preceding section, giving an almost constant value of  $R = (2.9 \pm 1.7) \times 10^{-7}$ . This value is two orders of magnitude lower than in  $\text{NaHDP}$  micelles, reflecting the higher water solubility of the product of hydrolysis.

The partial molar volume of  $\text{Na}_2\text{DP}$  micellized molecules was  $242.41 \pm 0.16 \text{ cm}^3 \text{ mol}^{-1}$  at  $25^\circ\text{C}$ . The distribution constant of  $\text{HDP}^-$  ions between micelles and intermicellar solution was  $K_d = 34 \pm 13$ , showing no significant dependence on  $C_T$ . It is evident that  $\text{HDP}^-$  ions

have only a slightly higher solubility in micelles over that in water, and the interaction between solubilize and micelles does not change with concentration. In contrast,  $\text{H}_2\text{DP}$  molecules have a very strong interaction with  $\text{HNaDP}$  micelles, with  $K_d$  ranging from  $2 \times 10^3$  to  $2 \times 10^7$  in the studied concentration range.

#### Effect of charge on cmc and micellization

The cmc values of aqueous solutions of  $\text{H}_2\text{DP}$ ,  $\text{HNaDP}$  and  $\text{Na}_2\text{DP}$  are given in Table 1. Cmc values are only slightly affected by temperature [16], so it may be concluded from the data of Table 1 that cmc increases by about one order of magnitude when the headgroup charge increases by one  $e$  unit.

Comparison between Figs. 2 and 6 showed that micelles of the 1:1 surfactant are more stable than that of 1:2. At concentrations larger than the cmc,  $\text{HNaDP}$  micelles grew speedily and the concentration of monomeric surfactant decreased strongly, whereas the concentration of  $\text{Na}_2\text{DP}$  micelles grew slowly and the concentration of the free surfactant was almost constant. On the basis of the theories about factors influencing micelle formation, this result is not surprising [26].

At the cmc,  $\text{HNaDP}$  micelles were less ionized ( $\alpha \approx 0.2$ ) than  $\text{Na}_2\text{DP}$  ones ( $\alpha \approx 1.4$ ). The behavior of  $\alpha$  when the concentration is increased is different: in  $\text{HNaDP}$  micelles  $\alpha$  first rose, passed through a maximum and then decreased, whereas in  $\text{Na}_2\text{DP}$   $\alpha$  decreased monotonically when the total concentration was increased. The latter is the normal behavior of  $\alpha$ . The behavior of  $\text{HNaDP}$  micelles may be associated with the hydrogen-bonded structure of the Stern layer, because other 1:1 common surfactants do not show this phenomenon.

Due to the lower solubility of  $\text{H}_2\text{DP}$ , the distribution constant of this product of hydrolysis is several orders of magnitude higher in  $\text{HNaDP}$  micelles than that of  $\text{HDP}^-$  ions in  $\text{Na}_2\text{DP}$  micelles. Solubilization of  $\text{H}_2\text{DP}$  molecules may stabilize  $\text{HNaDP}$  micelles and "dilute" the surface

**Table 1** CMC values of  $\text{H}_2\text{DP}$  and its mono and disodium salts

Surfactant	$T$ ( $^\circ\text{C}$ )	cmc ( $\text{mol dm}^{-3}$ )	Reference
$\text{H}_2\text{DP}$	26	$(5.4 \pm 2.4) \times 10^{-4}$	25
	20–80	0.00104	16
$\text{HNaDP}$	66	$(5.8 \pm 0.1) \times 10^{-3}$	This work
	80	$6.5 \times 10^{-3}$	16
$\text{Na}_2\text{DP}$	25	$(2.57 \pm 0.08) \times 10^{-2}$	This work
	25	0.0177	24
	60	0.0238	15
	60	0.0221	16

charge density, thus releasing some of the  $\text{Na}^+$  ions from the Stern layer. If a change in micelle structure occurs at  $C_T \approx 0.035 \text{ mol dm}^{-3}$ , such as a sphere-rod transition, the subsequent approximation of the headgroups may cause an increase in the surface charge density and the capture of counterions by the Stern layer. In addition to this phenomenon there is a normal reduction of the Debye length by an increase of the ionic strength ( $I$ ) in the intermicellar solution, when  $C_T$  increases.

The initial value of  $\alpha \approx 1.4$  corresponds to a neutralization of about the 30% of the total charge of the micelle ( $\alpha_{\text{max}} = 2$ ), whereas in the HNaDP–water system,  $\alpha \approx 0.2$

corresponds to the neutralization of about the 80% of the charge ( $\alpha_{\text{max}} = 1$ ). The very high value of  $\alpha$  in  $\text{Na}_2\text{DP}$  micelles near to the cmc is due to the high ionization of the headgroups and the low  $\text{HDP}^-$  content in micelles, which could not “dilute” the surface charge. The very rapid decrease of  $\alpha$  in the  $\text{Na}_2\text{DP}$ –water system with increasing total concentration is due to the very high value of  $I$ .

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